UG/1st Sem/PHS/H/21(CBCS)

UG 1st Semester Examination 2021

PHYSICS (Honours)

Paper : DC-1

[CBCS]

Full Marks : 25

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

- 1. Answer any *five* questions :
- (a) If $u\vec{a} = \vec{\nabla}v$, where u, v are scalar fields and \vec{a} is a vector field, then show that

$$\vec{a}. \vec{\nabla} \times \vec{a} = 0.$$

- (b) Show that the vector field $\vec{F} = 2xy\hat{\imath} + (x^2 + 2yz)\hat{\jmath} + (y^2 + 1)\hat{k}$ is conservative and find the scalar potential.
- (c) Find the total work done in moving a particle in a force field given by $\vec{F} = 3xy\,\hat{\imath} 5z\,\hat{\jmath} + 10x\,\hat{k}$ along the curve $x = t^2 + 1$, $y = 2t^2$, $z = t^3$ from t = 1 to t = 2.
- (d) If $\vec{A}(t)$ has a constant magnitude and $\left|\frac{d\vec{A}}{dt}\right| \neq 0$, then show that $\frac{d\vec{A}}{dt}$ is perpendicular to \vec{A} .
- (e) Use Stokes' theorem to show that the line integral of $\vec{F} = -y\hat{\imath} + x\hat{\jmath}$ around a closed curve in the *XY*-plane is twice the area enclosed by the curve.
- (f) Prove that $\nabla^2 r^n = n(n+1)r^{n-2}$.
- (g) Evaluate the integral $I = \int_0^{\frac{\pi}{2}} \cos t \, \delta\left(t \frac{\pi}{4}\right) dt$.

Time : Two Hours

 $2 \times 5 = 10$

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2. Answer any *three* questions :

3+2=5

(a) (i)State the Taylor series for functions of one variable.

(ii) Obtain the expression for Laplace's equations in spherical polar co-ordinates for a point in space described by the co-ordinates (r, θ, φ) .

(iii)What is the physical significance of $\vec{\nabla} \cdot \vec{B} = 0$? 1+3+1=5

(b) (i)Prove that $\iiint (\phi \nabla^2 \psi - \psi \nabla^2 \phi) dv = \iint (\phi \vec{\nabla} \psi - \psi \vec{\nabla} \phi) d\vec{s}.$

(ii) A scalar field is defined by $\phi = \phi(x, y)$. If $d\phi$ is a perfect differential then show that

$$\frac{\partial^2 \phi}{\partial x \partial y} = \frac{\partial^2 \phi}{\partial y \partial x}.$$

- (c) Evaluate the integral $\oint [(xy x^2)dx + x^2ydy]$ over the triangle bounded by the lines y = 0, x = 1 and y = x and hence verify Green's theorem in the plane. 5
- (d) Solve by the method of separation of variables:

$$3\frac{\partial U}{\partial x} + 2\frac{\partial U}{\partial y} = 0, \text{ where } U(x,0) = 4e^{-x}.$$

(e) Solve the differential equation:

 $xy^2dx + (2 + x^2y)dy = 0$ with the condition that, y (at x = 1) = 2.

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UG 1st Semester Examination 2021

PHYSICS (HONOURS)

Paper : DC- 2 [CBCS]

Full Marks : 25

Time : Two Hours

 $2 \times 5 = 10$

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

1. Answer any *five* questions :

- (a) If a force \vec{F} satisfies the relation $\vec{\nabla} \times \vec{F} = 0$, then show that the force field is conservative.
- (b) A circular disc of mass M and radius r is set rolling on a horizontal table. If ω be the angular velocity of the disc, show that its total energy is $\frac{3}{4}Mr^2\omega^2$.
- (c) Consider a rocket moving vertically upward against uniform gravity \vec{g} , that ejects gas with a constant velocity \vec{v} with respect to itself. Obtain the equation of motion of the rocket.
- (d) By using Euler's equations, show that the rotational kinetic energy of a rigid body is conserved when the applied torque is zero.
- (e) Derive gravitational field intensity due to a point mass M at a distance r from it, using Gauss's theorem of Gravitation.
- (f) Calculate the Poisson's ratio for silver, given Young's modulus for silver is 7.25×10^{10} N/m² and Bulk modulus is 11×10^{10} N/m².
- (g) What is Reynold's number? How is it used to determine whether the nature of flow of a liquid is streamline or turbulent?

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- 2. Answer any *three* questions :
- (a) Prove that the total energy of a particle of mass m moving under a central force is given by

$$E = \frac{h^2}{2m} \left[u^2 + \left(\frac{du}{d\theta}\right)^2 \right] + V(r)$$

where $u = \frac{1}{r}$, h = angular momentum of the particle and V(r) is the potential energy at r.

- (b) (i) The density of a sphere varies as the depth below the surface. Show that the gravitational attraction is greatest at a depth equal to 1/3 of the radius.
 - (ii) What do you understand by gravitational self-energy of a homogeneous sphere?

3+2=5

 $5 \times 3 = 15$

- (c) (i) A reference frame is rotating with an angular velocity $\vec{\omega}$ with respect to the laboratory frame. Establish the transformation relation $\frac{d}{dt} = \frac{d'}{dt} + \vec{\omega} \times$. How does a vector transform in such cases, if it is parallel to the axis of rotation?
 - (ii) Calculate the principal moments of inertia of a homogeneous cube of mass M and side a.

$$1+1+3=5$$

- (d) (i) Establish that shear is equivalent to elongation and contraction at right angles to each other. (ii) A metal rod of length *L* and cross-section α suffers a small longitudinal strain and is stretched by *l* in length. Show that the potential energy stored in the rod due to this strain is $(Y\alpha l^2)/2L$ if the Young's modulus of the material is *Y*. 3+2=5
- (e) (i) Write down the equation of continuity in case of fluid motion.

(ii) A capillary tube of radius *a* and length *l* is fitted horizontally at the bottom of a cylindrical flask of cross-section *A*. Initially, there is water in the flask up to a height h_1 . Show that the time $T = (8\eta l A / \pi \rho g a^4) \ln \frac{h_1}{h_2}$ is required for the height to be reduced from h_1 to h_2 . Here η is the coefficient of viscosity of water. 1+4=5